Linkage of XcalableMP and Python languages for high productivity on HPC cluster system

- Application to Graph Order/degree Problem -

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Background

- **XcalableMP (XMP)** is a directive-based language extension for HPC cluster systems
  - Provide directives for PGAS programming
  - Based on C and Fortran (C++ on the table)
  - Designed by PC Cluster consortium
  - http://xcalablemp.org

- **Omni compiler**
  - Reference implementation for XMP
  - Developed by RIKEN AICS and University of Tsukuba
  - Source-to-Source compiler
    - Support: The K computer, Intel Xeon Phi Cluster, Cray machines, ...
  - Open source software
  - http://omni-compiler.org
Example of XcalableMP programming

```c
int a[MAX];
#pragma xmp nodes p[3]
#pragma xmp template t[MAX]
#pragma xmp distribute t[block] onto p
#pragma xmp align a[i] with t[i]

int main(){
#pragma xmp loop on t[i]
   for(int i = 0; i < MAX; i++)
      a[i] = foo(i);
```

- Define execution unit and data distribution
- Parallelize loop statement
- Global address space
- Private address space
- Execution unit
Example of XcalableMP programming

```plaintext
integer a(MAX)
!$xmp nodes p(3)
!$xmp template t(MAX)
!$xmp distribute t(block) onto p
!$xmp align a(i) with t(i)

!$xmp loop on t(i)
do i = 1, MAX
  a(i) = foo(i)
enddo
```

Define execution unit and data distribution

Parallelize loop statement

Global address space
Private address space
Execution unit
Objective

- The purpose of a PGAS language is to develop parallel applications with both high productivity and performance.
- To do this, we think that a linking of a PGAS language and other languages is very important.
- Different programming languages are good at different things.

Why do we choose Python?
- Python has a lot of packages for fields of science (e.g. SciPy and NumPy).
- There are many users of Python.

Development function for a linkage of XMP and Python
Agenda from this slide

- Linkage of XMP and a C/Fortran program using MPI library
- Linkage of XMP and Python
  - Application to Graph Order/degree Problem
- Summary
Agenda from this slide

- Linkage of XMP and a C/Fortran program using MPI library
  1. Call an XMP program from a C/Fortran program using MPI library
  2. Call a C/Fortran program using MPI library from an XMP program

Why these function are needed?

1. While using XMP makes the code simple, performance may be slightly worse than MPI. We think that if necessary, it is important to use XMP and MPI properly in an application to achieve both high productivity and performance

2. Many other languages (e.g. Python, perl, ruby and so on) have MPI library. By creating a linkage XMP function with MPI, XMP can also link with other languages
A user code with XMP directives is translated to a parallel code with runtime calls of Omni compiler's runtime library.

- The **runtime library** is implemented in C and MPI.
- The translated parallel code is compiled by a native compiler (e.g. GNU, Intel, PGI, Cray, and so on).
Call XMP program from a program using MPI

- Implement following functions (which are defined in xmp.h)

<table>
<thead>
<tr>
<th>Language</th>
<th>Return Value Type</th>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>XMP/C</td>
<td>void</td>
<td>xmp_init(MPI_Comm)</td>
<td>Initialize XMP environment</td>
</tr>
<tr>
<td>XMP/F</td>
<td>(None)</td>
<td>xmp_init(Integer)</td>
<td></td>
</tr>
<tr>
<td>XMP/C</td>
<td>void</td>
<td>xmp_finalize(void)</td>
<td>Finalize XMP environment</td>
</tr>
<tr>
<td>XMP/F</td>
<td>(None)</td>
<td>xmp_finalize()</td>
<td></td>
</tr>
</tbody>
</table>

A program using MPI (mpi.c)
```c
#include <xmp.h>
#include <mpi.h>

int main(int argc, char **argv){
  MPI_Init(&argc, &argv);
  xmp_init(MPI_COMM_WORLD);
  call_xmp();
  xmp_finalize();
}
```

XMP program (xmp.c)
```c
void call_xmp(){
  #pragma xmp nodes p[3]
}
```

$ xmpcc xmp.c -c
$ mpicc mpi.c -c
$ xmpcc xmp.o mpi.o -o a.out
$ mpirun -np 3 a.out
Call a program using MPI from XMP program

- Implement following functions (which are defined in xmp.h)

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<tr>
<td>XMP/C</td>
<td>void</td>
<td>xmp_init_mpi(int*, char***)</td>
<td>Initialize MPI environment</td>
</tr>
<tr>
<td>XMP/F</td>
<td>(None)</td>
<td>xmp_init_mpi()</td>
<td></td>
</tr>
<tr>
<td>XMP/C</td>
<td>MPI_Comm Integer</td>
<td>xmp_get_mpi_comm(void)</td>
<td>Create MPI communicator from XMP node set</td>
</tr>
<tr>
<td>XMP/F</td>
<td>(None)</td>
<td>xmp_get_mpi_comm()</td>
<td></td>
</tr>
<tr>
<td>XMP/C</td>
<td>void</td>
<td>xmp_finalize_mpi(void)</td>
<td>Finalize MPI environment</td>
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<td>(None)</td>
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</table>

**XMP program (xmp.c)**

```c
#include <xmp.h>
#include <mpi.h>
#pragma xmp nodes p[3]

int main(int argc, char **argv){
    xmp_init_mpi(&argc, &argv);
    MPI_Comm comm = xmp_get_mpi_comm();
    call_mpi(comm);
    xmp_finalize_mpi();
}
```

**A program using MPI (mpi.c)**

```c
#include <mpi.h>

void call_mpi(MPI_Comm comm){
    int rank, size;
    MPI_Comm_rank(comm, &rank);
    MPI_Comm_size(comm, &size);
}
```

$ xmpcc xmp.c -c
$ mpicc mpi.c -c
$ xmpcc xmp.o mpi.o -o a.out
$ mpirun -np 3 a.out
Agenda from this slide

- Linkage of XMP and a C/Fortran program using MPI library
- Linkage of XMP and Python
  - Application to Graph Order/degree Problem
- Summary
Linkage of XMP and Python

1: Parallel Python program calls a parallel XMP program
   - This concept is the same as that of XMP and a program with MPI

2: Serial Python program calls a parallel XMP program
Parallel Python program calls a parallel XMP program

```python
import xmp
from mpi4py import MPI

lib = xmp.Lib("xmp.so")
args = ([1,2,3], [4,5,6])
job  = lib.call(MPI.COMM_WORLD, "call_xmp", args)
```

- `xmp.Lib()` sets "shared library" which is developed in XMP program
- `xmp.Lib.call()` executes an XMP program
  - `xmp.Lib.call()` calls "xmp_init()" and "xmp_finalize()" internally

```
void call_xmp(long a1[3], long a2[3]){
#pragma xmp nodes p[3]

Python program (a.py)

XMP program (xmp.c)
```

$ xmpcc -fPIC -shared xmp.c -o xmp.so
$ mpirun -np 3 python a.py
Serial Python program calls a parallel XMP program

Python program (a.py)

```python
import xmp
lib = xmp.Lib("xmp.so")
args = ([1,2,3], [3,4,5])
job = lib.spawn(3, "call_xmp", args)
```

XMP program (xmp.c)

```c
void call_xmp(long a1[3], long a2[3]){
#pragma xmp nodes p[3]
}
```

- `xmp.Lib.spawn()` method creates new processes and they work as an XMP program in parallel

```
$ xmpcc -fPIC -shared xmp.c -o xmp.so
$ mpirun -np 1 python a.py
```
Serial Python program calls a parallel XMP program

Python program (a.py)

```python
import xmp

lib = xmp.Lib("xmp.so")
args = ([1,2,3], [3,4,5])
job = lib.spawn(4, "call_xmp", args, async=True)
// other work
job.wait()
```

XMP program (xmp.c)

```c
void call_xmp(long a1[3], long a2[3]){
#pragma xmp nodes p[3]

```

- `xmp.Lib.spawn()` method creates new processes and they work as an XMP program in parallel.

```

$ xmpcc -fPIC -shared xmp.c -o xmp.so
$ mpirun -np 1 python a.py

```
Implementation of xmp.Lib.spawn()

1. User program calls xmp.Lib.spawn()
2. xmp.Lib.spawn() creates **Intermediate program** automatically and executes **Intermediate program** using the spawn method of mpi4py
3. xmp.Lib.spawn() broadcasts the arguments to **Intermediate program** using mpi4py.Bcast()
4. **Intermediate program** receives the arguments
5. **Intermediate program** executes an XMP program (This procedure is the same as parallel run style)

```
import mpi4py
import numpy
from ctypes import *

comm = MPI.COMM_WORLD
arg0 = numpy.zeros(2)
comm.Bcast(arg0, root=0)
lib = CDLL("xmp.so")
lib.xmp_init_py(comm.py2f())
lib.call_xmp(arg0.ctypes)
lib.xmp_final()
comm.Disconnect()
```
Agenda from this slide

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- Summary
What is Graph Order/degree problem?

- Minimizes the "diameter" and "average shortest path length (ASPL)" among vertices in an undirected graph with "a given number of vertices and degrees".
- The problem is useful for designing low latency interconnection networks.
- Although the smallest diameter and ASPL can be calculated from the given vertices and degrees [V.G.Cerf 1974], we don't know how edges and vertices are connected.
- Examples of the graph with vertices = 10 and degree = 3.

Diameter=3, ASPL=1.89 (Random)  Diameter=2, ASPL=1.67 (Optimal)
What is Graph Order/degree problem?

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- The problem is useful for designing low latency interconnection networks.
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- Examples of the graph with vertices = 10 and degree = 3
Graph Golf@National Institute of Informatics

- National Institute of Informatics has held the Graph Golf competition since 2015 for Graph Order/degree problem.
- http://research.nii.ac.jp/graphgolf
- Some combinations of vertices and degrees are provided

Combination of vertices and degrees of General Graph Category in 2017

<table>
<thead>
<tr>
<th>Number of vertices ($n$)</th>
<th>32</th>
<th>256</th>
<th>576</th>
<th>1344</th>
<th>4896</th>
<th>9344</th>
<th>88128</th>
<th>98304</th>
<th>100000</th>
<th>100000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of degrees ($d$)</td>
<td>5</td>
<td>18</td>
<td>30</td>
<td>30</td>
<td>24</td>
<td>10</td>
<td>12</td>
<td>10</td>
<td>32</td>
<td>64</td>
</tr>
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Problem statement

Definition

The order/degree problem with parameters $n$ and $d$: Find a graph with minimum diameter over all undirected graphs with the number of vertices $n$ and degree $d$. If two or more graphs take the minimum diameter, a graph with minimum average shortest path length (ASPL) over all the graphs with the minimum diameter must be found.

The order/degree problem on a grid graph with a limited edge length $r$: Do the same as above, but on a $\sqrt{n} \times \sqrt{n}$ square grid in a two-dimensional Euclidean space, keeping the lengths of the edges $r$ in Manhattan distance. Here a "grid" implies that (1) the vertices are located at integer coordinates but are not necessarily connected to its adjacent vertices; and (2) the edges must not run diagonally while being allowed to change its direction at the grid points.
Usage of XMP

- A python program for the Graph Golf competition is available on the official website
  - http://research.nii.ac.jp/graphgolf/py/create-random.py (About 100 lines)
- The python program outputs follow from the number of vertices and degrees.
  - Initial graph with random edges
  - Calculation of diameter and ASPL
  - The graph is saved in PNG format
- Python "networkx" package is used
  - https://github.com/networkx/

- Issues
  - The python program doesn't search the smallest diameter and ASPL
  - To calculate diameter and ASPL, it requires a significant amount of time

We create an XMP program to solve the issues.
Graph Order/degree solver in Python + XMP

- **Implementation policy**
  - The existing python program generates an initial solution and saves a final solution.
  - XMP program searches an optimal solution (including calculates diameter and ASPL).
  - Optimization algorithm in XMP uses Simulated Annealing.

Python
```
import xmp

lib = xmp.Lib("xmp.so")
args = (vertices, degrees, edge)
lib.spawn(1280, "xmp_sa", args)
```

XMP/C
```
void xmp_sa(int vertices, int degrees,
            int edge[vertices*degrees/2][2]){
    #pragma xmp loop on t[i]
    for(int i=0;i<vertices;i++){
        // Calculate diameter and ASPL
    }
    #pragma xmp reduction(max:diameter)
    #pragma xmp reduction(+:ASPL)
```
Evaluation

- COMA cluster system at University of Tsukuba

<p>| | |</p>
<table>
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<tbody>
<tr>
<td>CPU</td>
<td>Intel Xeon-E5 2670v2 2.8 GHz x 2 Sockets</td>
</tr>
<tr>
<td>Memory</td>
<td>DDR3 1866MHz 59.7GB/s 64GB</td>
</tr>
<tr>
<td>Network</td>
<td>InfiniBand FDR 7GB/s</td>
</tr>
<tr>
<td>Software</td>
<td>intel/16.0.2, intelmpi/5.1.1, Omni Compiler 1.2.1, Python 2.7.9, networkx 1.9</td>
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- Elapse time to calculate diameter and ASPL
- Problem size is vertices=9344, degrees=10

Combination of vertices and degrees of General Graph Category in 2017

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Performance results

- flat-MPI
- 20 processes in a single compute node
- The python code using networkx package requires 148.83 sec.

![Graph showing execution time and parallel efficiency](image)

921 times faster
Conclusion

- Since different programming languages are good at different things, we developed the linkage function for XMP and Python.
  - Parallel python program calls a parallel XMP program.
  - Serial python program spawns new processes which executes a parallel XMP program.
- Development of an application of the Graph Order/degree problem using the linkage function.
  - As a result of using 1280 CPU cores, it achieved 921 times faster than using 1 CPU core.
  - Python networkx package is used to create an initial graph and save a final graph.
  - By mixing Python and XMP, the parallel application is developed easily.